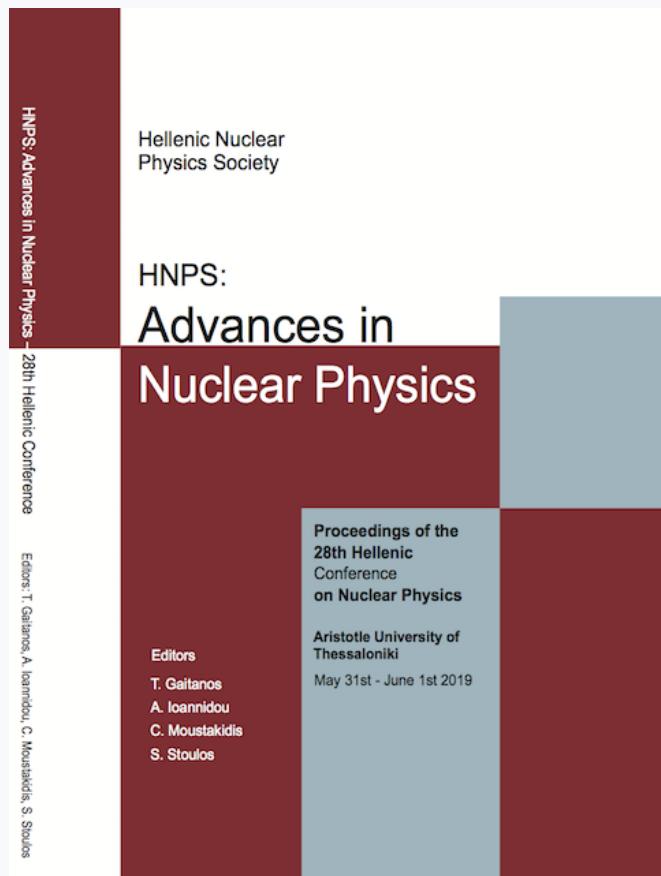


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*Canel Eke, A. Yildirim*

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# Investigation of Photon Attenuation Properties of CR-39 Lens

C. Eke<sup>1</sup>, A. Yildirim<sup>2</sup>

<sup>1</sup> Akdeniz University, Faculty of Education, Department of Mathematics and Science Education, Division of Physics Education, 07058, Antalya, Turkey

<sup>2</sup> Akdeniz University, Faculty of Science, Department of Physics, 07058, Antalya, Turkey

**Abstract** The purpose of this study is to investigate photon attenuation parameters of Colombia Resin-39 (CR-39) lens, which are linear attenuation coefficient (LAC), mass attenuation coefficient (MAC), half value layer (HVL), tenth value layer (TVL), mean free path (MFP), effective atomic number ( $Z_{eff}$ ) and effective electron density ( $N_{eff}$ ). MACs were determined theoretically and with simulation in the energy range from 0.01 to  $10^5$  MeV. Also, obtained MACs of CR-39 lens were compared with MACs of pure aluminum and lead. Theoretically obtained  $Z_{eff}$  values were compared with  $Z_{eff}$  results obtained by the computer software.

The results of this study are; a) the theoretically obtained MACs values are in agreement with MACs obtained results from simulation software, b) the theoretically obtained  $Z_{eff}$  values are in agreement with  $Z_{eff}$  obtained by the computer software c) the MACs of CR-39 lens are much lower than MACs of pure lead whereas there is not too much differences between MACs of CR-39 and pure aluminum d) the HVLs, TVLs and MFPs rise with increasing photon energy while the LACs and MACs reduce with increasing photon energy.

**Keywords** mass attenuation coefficient, gamma-ray spectrometry, CR-39 lens

Corresponding author: C. Eke (ceke@akdeniz.edu.tr) | Published online: May 1<sup>st</sup>, 2020

## INTRODUCTION

Exploring the gamma-ray properties of the different materials and compounds are significant because gamma-rays are used in various objectives such as nuclear power plants, radiation dosimetry, medicine, industry, shielding, etc. [1-4]. Protection from the ionizing radiation effect is necessary for the humans because it causes distortion on the biological, atomic, molecular structure of the materials [5].

Gamma-rays interact with matter as photoelectric effect, Compton scattering and pair production and it depends on incident photon energy and structure of the absorber material. Photoelectric effect is dominant at low gamma-ray energies whereas pair production is dominant at high gamma-ray energies especially greater than 1022 keV. Compton scattering is prominent in the mid-photon energy range [6].

The gamma-ray attenuation parameters which are linear attenuation coefficient (LAC), mass attenuation coefficient (MAC), total atomic cross section ( $\sigma_a$ ), total electron cross section ( $\sigma_e$ ), effective atomic number ( $Z_{eff}$ ) and effective electron density ( $N_{eff}$ ), half value layer (HVL), tenth value layer (TVL), mean free path (MFP) are significant to decide the effects of the gamma-rays in matter [7]. These parameters can be determined by experimentally, theoretically and computer simulation [8,9].

The attenuation parameters of many different materials such as soil, oil-soil samples [10], raw wood and binderless particleboards of Rhizophora spp. [11], carbohydrates, (Esculin, Sucrose, Sorbitol, D-Galactose, Inositol, D-Xylose) [12], some vitamins (retinol, beta-carotene, thiamine, riboflavin, niacinamide, pantothenic acid, pyridoxine, biotin, folic acid, cyanocobalamin, ascorbic acid, cholecalciferol, alpha-tocopherol, ketamine, hesperidin) [13], some building materials [14], different

types of glasses [15-17], some polymers (polyoxymethylene, poly acrylonitrile, natural rubber, polyethyl acrylate, polyphenyl methacrylate, and polyethylene tetraphthalate) [18-20], plastic [20-21] have been investigated in the scientific literature by the researchers.

In this study, Columbia Resin 39 (CR-39) plastic polymer having chemical composition  $C_{12}H_{18}O_7$  which is called allyl diglycol carbonate [22-24] was investigated. CR-39 is generally used for nuclear reaction physics, radon dosimetry, radiobiological measurements as nuclear track detectors and production of the eyeglass lenses [24,25].

The aim of this study is to investigate attenuation parameters of gamma radiation which are MACs, LACs, HVLs, TVLs, MFPs, atomic cross section, electron cross section  $Z_{eff}$  and  $N_{eff}$  of the CR-39 lens. The theoretically obtained MACs of CR-39 lens have been compared with the MACs obtained by the simulation code. Also theoretically obtained MACs of CR-39 lens have been compared with MACs of the Aluminium and lead. Theoretically obtained  $Z_{eff}$  values have been compared  $Z_{eff}$  values obtained by the computer software.

## THEORETICAL CALCULATIONS

The linear attenuation coefficient (LAC) and mass attenuation coefficient (MAC) of CR-39 lens were calculated using the Beer Lambert law as following equations [6]:

$$I = I_0 e^{-\mu x} \quad (1)$$

$$\mu_m = \frac{\mu}{\rho} \quad (2)$$

where  $\mu$  and  $\mu_m$  are LAC and MAC of the absorber, respectively,  $x$  is the thickness of the sample,  $\rho$  is the density of the absorber,  $I$  is counts of per seconds of point sources with absorber and  $I_0$  is counts of per seconds of point sources without absorber.

The MACs are calculated for mixtures and components considering basic ingredients of the absorber by using following equation [26]:

$$\mu_m = \frac{\mu}{\rho} = \sum_i w_i \left( \frac{\mu}{\rho} \right)_i \quad (3)$$

where  $w_i$  is the weight fraction of the atomic components and  $\left( \frac{\mu}{\rho} \right)_i$  is the MAC of the  $i^{th}$  element.  $\left( \frac{\mu}{\rho} \right)_i$  at all the absorption edges of all the components of the elements are calculated using interpolation for the atomic photoeffect cross section, coherent (Rayleigh) and the incoherent (Compton) scattering cross sections, cross sections for electron-positron production in the fields of the nucleus and of the atomic electrons also including the photoeffect cross sections for the individual atomic subshells [26].

In this study MACs of the CR-39 lens were calculated theoretically using WinXCom software [27]. WinXCom is Windows version of XCOM which was developed by the Berger and Hubbell [28] for computing MACs or photon interaction cross-sections for any element, compound or mixture at energies from 1 keV to 100 GeV [27].

In following equation 4 and 5 represent total atomic cross section per atom  $\sigma_a$  ( $\text{cm}^2/\text{atom}$ ) and total electronic cross section per electron  $\sigma_e$  ( $\text{cm}^2/\text{electron}$ );



$$\sigma_a = \frac{1}{N} \frac{(\mu/\rho)_{material}}{\sum_i \frac{w_i}{A_i}} \quad (4)$$

$$\sigma_e = \frac{1}{N} \sum_i \frac{f_i A_i}{Z_i} \left( \frac{\mu}{\rho} \right)_i \quad (5)$$

where  $N$  is the Avogadro's number,  $A_i$  is the atomic weight of the  $i^{th}$  element,  $w_i$  is fractional weight,  $f_i$  is the molar fraction of the  $i^{th}$  element and  $Z_i$  is the atomic number of the  $i^{th}$  element [3,11].

Effective atomic number  $Z_{eff}$  is calculated using following equation [3,11]:

$$Z_{eff} = \frac{\sigma_a}{\sigma_e} \quad (6)$$

Effective electron density  $N_{eff}$  (electron/g) is related with  $(Z_{eff})$  and it is calculated using following equation [3,11]:

$$N_{eff} = \frac{(\mu/\rho)_{material}}{\sigma_e} \quad (7)$$

The HVL, TVL and MFP are calculated as follows [29,30]:

$$HVL = \frac{\ln 2}{\mu} \quad (8)$$

$$TVL = \frac{\ln 10}{\mu} \quad (9)$$

$$MFP = \frac{1}{\mu} \quad (10)$$

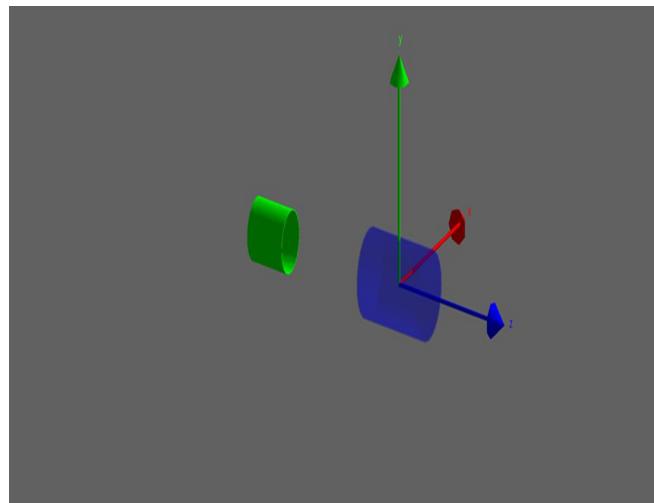
## SIMULATION PROCEDURE

Geant4 simulation toolkit is used for the simulation of mass attenuation coefficients [31-33]. Geant4 is a very powerful simulation software and currently used by many researchers around the world. It is one of the best simulation programs to investigate the particles passing through matter. It is used in the areas of nuclear physics, high energy physics, accelerator physics, medical physics and space sciences. There are many collaborators still developing the software. Research groups also create libraries for their own works which are contribute the developing of the toolkit. For this study Livermore library (Low Energy Electromagnetic Physics), which is an official Geant4 library, was used to determine the mass attenuation coefficients.

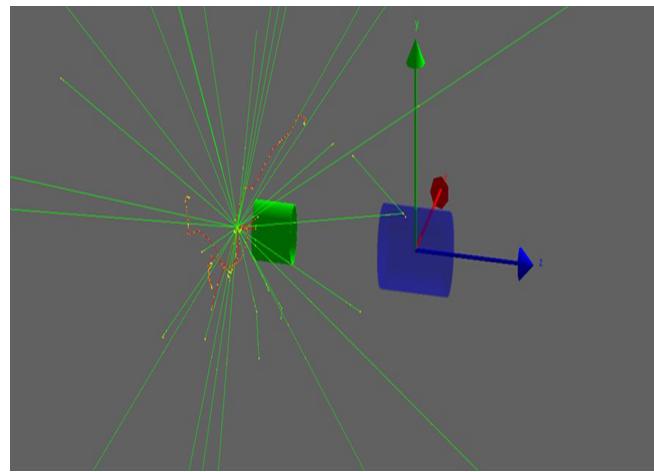
Using Geant4, one can calculate the attenuation coefficients by either directly from desired material or simply creating the experiment conditions and counting photons that reached the detector via code blocks. For both cases the results are almost the same. In this study we used the latter one. The lens and the detector are shown in Fig. 1.

In Fig. 1, the green cylinder is the lens sample and the blue cylinder is the HPGe detector. The axes are shown with arrows. Like a real experiment, simulations were done with and without the sample to calculate the attenuation coefficients. In Fig. 2, it is shown the gamma-ray interactions with the sample and the detector. Gamma-rays are propagating along all space from a point source. The source is placed just in front of the sample. The simulation was taken place in air. There is nothing else in the simulation setup for the gamma rays to interact and change the results.

Obtained results were discussed in the next section along with the theoretical ones.



**Figure 1.** Graphical demonstration of experiment setup

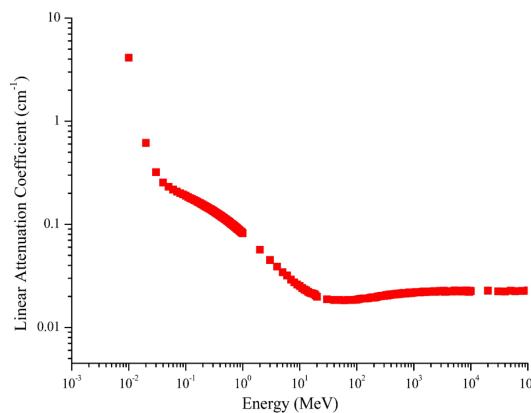


**Figure 2.** The point source and the interactions of gamma rays with sample and detector

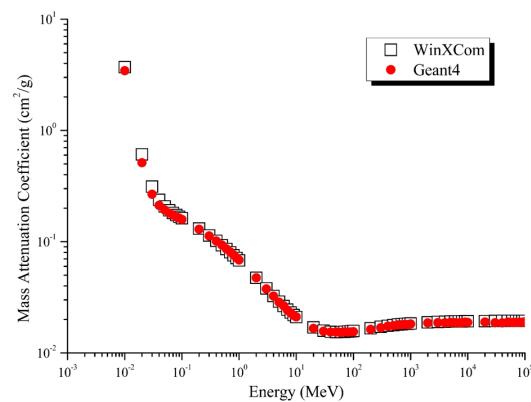
## RESULTS AND DISCUSSION

The variation of LACs and comparison MACs between WinXCom [27] and Geant4 [31-33] of CR-39 lens are shown in Fig. 3 and Fig. 4, respectively. Also, obtained MACs of CR-39 were compared the MACs of pure aluminum (*Al*) and lead (*Pb*) which are commonly used as shielding materials (see Fig. 5).

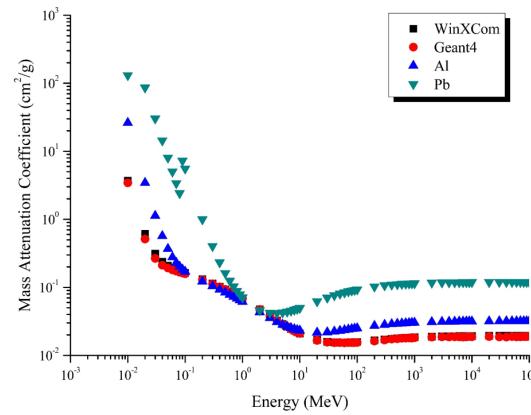
The MAC gives information about evaluating of the mean number of the interactions between incident photons and material which take place in a dedicated mass-per-unit field thickness of the investigated matter. The MAC is free of the density and physical situation of the absorber therefore it is more significant than the LAC [20]. As shown in Fig. 3, 4 and 5, the LACs and MACs decrease with increasing photon energy and it tends to be stable at higher photon energies because photoelectric effect is dominant at low photon energies, Compton scattering takes place at intermediate photon energies whereas pair production replaces at higher photon energies [7]. The theoretically obtained MACs by using WinXCom are agreement with obtained MACs by the Geant4 simulation software (see Fig. 2). The MACs of CR-39 are agreement with *Al* whereas the MACs of CR-39 are lower than *Pb* especially at low and high photon energies as shown in Fig. 5.



**Figure 3.** Variation of LACs versus photon energies



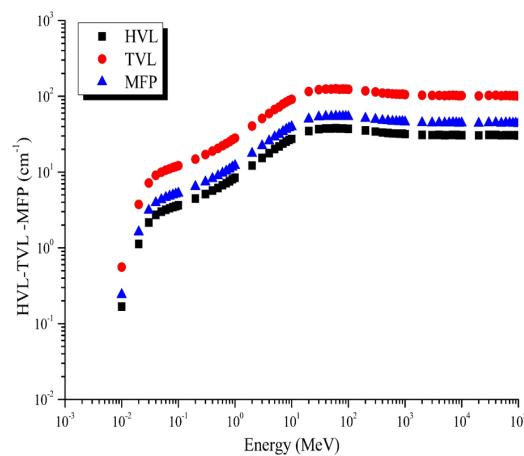
**Figure 4.** Variation of MACs versus photon energies



**Figure 5.** Comparison of MACs of CR-39, Al and Pb versus photon energies

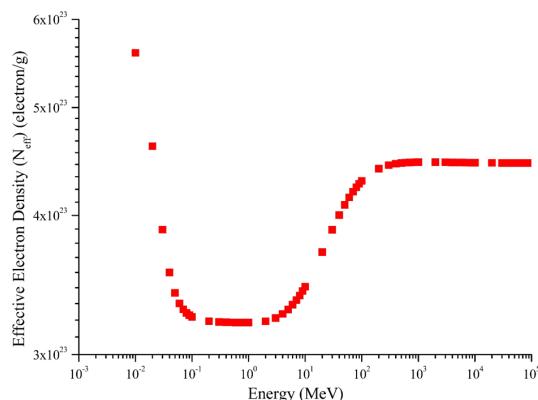
Variations of HVLs, TVLs and MFPs versus photon energies as shown in Fig. 6. The HVL, TVL and MFP of CR-39 increase with increasing photon energies. The HVL and TVL are described as the thickness of the absorber which decreases the intensity by a factor of two and ten, respectively which are required for the radiation dosimetry evaluations. The MFP is average distance of a two successive

photons where reduces 63% of the total intensity will interact [30]. The HVL and TVL of the absorber should be small for the strong radiation shielding [29].



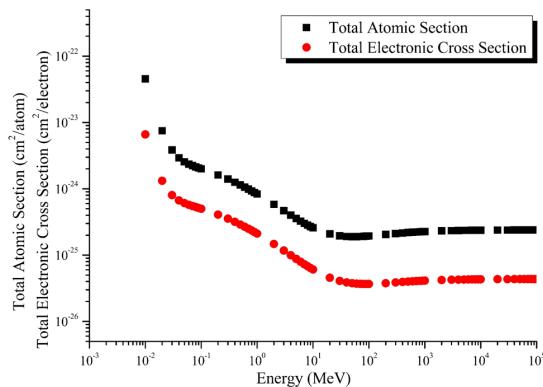
**Figure 6.** Variation of HVLs, TVLs and MFPs versus photon energies

$Z_{\text{eff}}$  and  $N_{\text{eff}}$  are used to define for the compounds and mixtures because the atomic number of compounds and mixtures can not be described with single atomic number against to incident photon energy.  $N_{\text{eff}}$  and  $Z_{\text{eff}}$  (see Fig. 7 and Fig. 9) depend on the incident photon energy also  $Z_{\text{eff}}$  is ratio of the total electron cross section to total electronic cross section and  $N_{\text{eff}}$  is the number of electrons per unit mass [5-34].

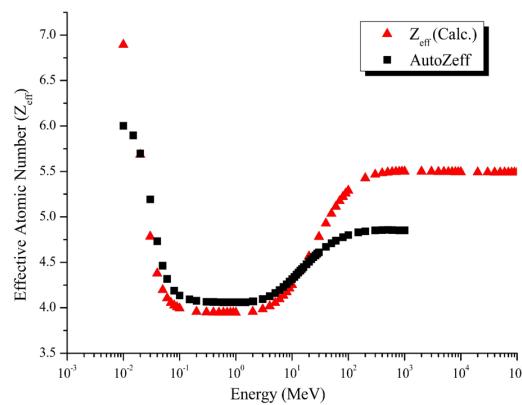


**Figure 7.** Variation of effective electron densities versus photon energies

Variation of effective electron density, total atomic cross section, total electronic cross section and effective atomic number versus photon energies are presented in Fig. 7, 8 and 9, respectively. The  $Z_{\text{eff}}$  values obtained using MACs values from WinXCom are in agreement with obtained  $Z_{\text{eff}}$  values from AutoZeff software [35]. The  $N_{\text{eff}}$  and  $Z_{\text{eff}}$  sharply decreases at low photon energies, it tends to be stable at intermediate energies then these parameters increase again and tends to be constant at higher photon energies. The reason of this process is interaction of photons with matter as photoelectric effect, Compton scattering and pair production. Especially, intermediate photon energies Compton scattering is effective and cross section of the Compton scattering varies linearly with atomic number [5].



**Figure 8.** Variation of total atomic cross section and total electron cross section versus photon energies



**Figure 9.** Variation of effective atomic numbers versus photon energies

## CONCLUSIONS

In this study, radiation shielding parameters which are LACs, MACs, HVL, TVL, MFP,  $Z_{\text{eff}}$  and  $N_{\text{eff}}$  were calculated. The MACs were determined theoretically and with simulation in the energy range from 0.01 to  $10^5$  MeV. It was concluded that theoretically obtained MACs values of CR-39 lens were agreement with values obtained from Geant4 simulation software. The MACs of CR-39 lens were nearly equal to MACs of aluminum. The MACs of CR-39 lens were nearly equal to MACs of Aluminum though these values were lower than MACs of lead. The LACs, MACs, total atomic cross section and total electronic cross section decrease with increasing photon energies whereas HVLs, TVLs and MFPs rise with increasing photon energies. Theoretically obtained  $Z_{\text{eff}}$  values were compared with  $Z_{\text{eff}}$  values obtained from AutoZeff software. It was deduced that theoretically calculated  $Z_{\text{eff}}$  values are close to obtained  $Z_{\text{eff}}$  values from AutoZeff software especially low and medium photon energies but there was significant differences at higher than 100 MeV.

In the future, the LACs and MACs can be calculated as experimentally and obtained results can be compared with theoretical and simulation results of CR-39 lens.

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